

MULTI-OBJECTIVE OPTIMIZATION OF A PM AIDED SYNCHRONOUS AVERSENESS MACHINE FOR LIGHT EV

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Abstract

Synchronous Reluctance (SynRel) machines are considered a competitive alternative to the induction motors for variable speed drive applications due to their comparable performance and low cost. The absence of rare earth permanent magnets makes them very attractive also in the automotive sector especially for light electric vehicles. The design of SynRel machines has been formalized by many authors in the last three decades but it is still an open challenge since it involves many competitive design objectives and a higher number of geometrical variables compared to other kind of machines. This paper is focused on the joint optimization of both stator and rotor of a SynRel machine with the aim of obtaining the highest torque density with the minimum iron and joule losses as well as smooth torque. The aim is to carry out a machine design that suits best the requirements of a small electric car for urban mobility, i.e. 30 kW with a base speed of 3000 rpm and a maximum speed of 6000 rpm. The proposed optimization strategy is global because it considers a geometry design that takes into account several stator and rotor parameters together. The design method consists in a two steps procedure: in the first stage the torque density and the losses are optimized, while the quality of the torque profile is improved in the second design stage. The results, satisfying the project requirements, are presented and compared to the initial reference machine. Finally a comparison between two design approaches allowing the improvements of the constant power speed range is presented and discussed.

Introduction

Synchronous reluctance machines have recently gained increasing interest both in industry and academia because of their excellent features, such as simple and robust rotor structure, high overload capability, high efficiency and low cost due to absence of permanent magnets [1]. It has been demonstrated that with respect to traditional induction motors, SynRel machines are showing comparable torque density and lower rotor losses due to the

absence of rotor copper losses [2]. Despite these advantages, the main drawbacks of SynRel motors are the high torque ripple and a poor power factor [3]. The first is not acceptable for most applications due to the direct effects on noise and vibration. The challenge of reducing the torque ripple has been extensively investigated during the past twenty years' research, and quite a number of techniques have been proposed with this aim [4]. It has been proved how the torque oscillations could be

minimized through different techniques: rotor skewing, suitable choice of the number of flux barriers with respect to the number of stator slots [5] and through the optimization of the flux barrier geometry [6]. The introduction of permanent magnets in the rotor flux barriers, even with a small amount of ferrite (Fig. 1), is beneficial for the improvement of the power factor as well as for the constant power speed range [7]. Although the analytical modelling and design of SynRel machines have been formalized by many authors in the last three decades [8, 9], such models are typically used during the preliminary design stage. They are obviously based on hypothesis in order to simplify their modelling and restrict the design space dimension.

Consequently, the design procedure of such machines is usually divided in two steps: first an analytical model is used to carry out a preliminary design and then a Finite Element Analysis (FEA) is employed to evaluate the design aspects disregarded in the first stage. The number and the influence of such neglected aspects depend on the accuracy and on the initial hypothesis of the considered analytical model. During the finite element refinement stage several design iterations can be needed. The computational time decreases as the accuracy of the analytical model used in the preliminary design increases. In recent works [10-12], automated design procedures assisted by optimization algorithms and coupled with FEA have been presented as an alternative of the aforementioned two steps design procedure. Those design strategy do not make use of any hypothesis and therefore have the advantages of considering all the

design aspects during the performance evaluations such as the non-linearities which have a strong impact on the behaviour of SynRel machines.

Proposed method

The methodology makes use of a stochastic optimization algorithm and finite element analysis. Particular attention has been paid to reduce the computational burden through a careful subdivision of the design procedure. This consists in two steps: first the main parameters affecting torque density and losses are optimized by a means of static FE simulations while in the second step, the variables which mainly influence the torque ripple are optimized through transient FE simulation. It has been proved that such approach considerably decreases the computational time and the goal of reducing the torque ripple has been achieved.

Methodology

Optimization strategy

The general design procedure of an electrical machine depends on the considered machine topology and on the initial constraints given by the specific application. In this study the main aim is to design a SynRel machine with the highest torque density without any envelope constraints and the minimum losses and torque ripple. The accurate evaluation of these objectives would require a considerable amount of FE simulations and therefore computational time. In fact, the accurate calculation of the torque profile requires a set of FE simulations over one sixth of the electrical period while the evaluation of the iron losses needs the FE simulation of a full electrical period. However in a first design stage, the torque density and the total losses Goule

and iron) can be estimated by means of static FE simulations for each machine candidate; during this step several static FE simulations are carried out in order to evaluate the maximum torque per phase angle (MTPA). In the second refinement design stage the torque profile can be calculated with a set of FE simulations over one sixth of the electrical period at the MTPA previously determined. In order to apply such methodology the design space is split in two subspaces:

1. in the first design step, the optimization focuses on the first subspace which contains the geometrical parameters that mainly affect the torque density and the losses, i.e. external diameter (D_e), stack length (L_{stk}), split ratio ($SR = D_e / D_{se}$), slot geometry (W_t , l_t) and insulation ratio (k_{atr}) as defined in [16];

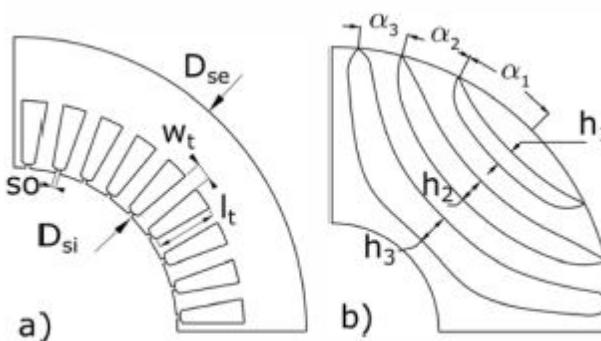


Figure 2: a) Stator parametrization, b) Rotor parametrization

2. In the second one, the optimization focuses on the second subspace which mainly affects the torque ripple, i.e. rotor flux barrier geometry (angular displacements at the airgap of the barrier $\alpha_{1,2,3}$ and the insulation ratio k_{atr}) and slot opening width (so), see Fig. 2. It is worth to underline that several assumptions have to be made for each design step, in particular:

- in the first design step, the distribution of the angular displacements at the airgap of

the flux barriers is preliminary identified according to [17]; moreover the slot opening (so) is fixed to 0.3 pu;

- in the second design step, the main stator parameters are kept constant and equal to the optimum values obtained in the first step whereas the angular displacements at the airgap of the flux barriers, the insulation ratio and the slot opening width are refined.

The per-unit parametrizations of the stator and rotor variables are shown in Fig. 1 and have been defined respectively in [18,19]. A stator configuration with a 36-slot 4-pole distributed winding is considered along with a rotor structure with three flux barriers per pole. Regarding the geometry of the flux barriers, several alternatives have been presented in literature. It has been shown [21] that adopting a flux barrier profile which follows the flux lines that the stator winding would produce in a solid rotor (i.e. laminated rotor without barriers) gives better electromagnetic performance. The latter geometry has been adopted in this work. The current density in the slot is set to 9 A/mm² and the torque requirement is reached up to the base speed of 2500 rpm. The iron losses are computed considering a slot fill factor of 0.4 and the length of the end windings which is proportional to the external diameter of the stator and to the coil pitch. The iron losses have been estimated according to the following expression:

$$P_{fe} = \rho_{fe} \left(\frac{B_{max}}{B_{ref}} \right)^2 \left[k_{hy} \left(\frac{f}{f_{ref}} \right) + k_{ed} \left(\frac{f}{f_{ref}} \right)^2 \right]$$

Where the maximum flux densities are extracted from the field solution in the different parts of the machine. The coefficients k_{hy} , k_{ed} are the hysteresis and

eddy current constants respectively. Their value is depending on the lamination properties and (M290) and has been carried out through datasheet curve fitting.

Results

Optimization results

A. Torque density, joule and iron losses optimization Torque density, iron losses and joule losses are the objectives of the first design step. Those performance indexes have been evaluated by means of static FE simulations carried out for different current phase angles in order to identify the MTP A which is a-priori unknown and obviously the maximum torque. Table I depicts the limit of the design variables used during the optimizations. Two additional constraints have been considered throughout the design procedure: 1) the maximum flux densities in the tooth and in the back iron have been constrained to be less than 1.85 and 1.65 [T] respectively, 2) the maximum torque has to be in the range 90-150 Nm. Fig. 3 shows the Pareto front of the optimization in the plane iron losses – joule losses with the torque density represented by the colour scale. It is clear the trade-off between total losses and torque density: as the losses increases, the torque density grows. In particular, a 60% increment of losses causes a 25% increment of torque density. For a given value of total losses, several designs having slightly different distribution of the losses are available; however those differences are almost negligible and are due to the different magnetic saturations of those solutions. Four different designs have been picked up from the Pareto front and analysed in details as shown in Table II

and III. Those four designs correspond to four different cooling capabilities; in fact the ratio between the total losses and the external stator surface areas k_j increases as the torque density increases as shown in table III. The optimal machines show the same split ratios and stack length and almost the same insulation ratio and slot geometry. They differ for the external diameter and

Table I: Design variables boundaries

Parameter	Lower limit	Upper limit	Unit
D_{sc}	100	400	mm
L_{st}	50	300	mm
SR	0.35	0.75	p.u.
$I_{t, pu}$	0.3	0.8	p.u.
$W_{t, pu}$	0.3	0.8	p.u.
k_{air}	0.35	0.55	p.u.
α_1	15	19	deg.
α_2	26	30	deg.
α_3	36	40	deg.
k_{air}	0.4	0.5	p.u.
so	0.2	0.8	p.u.

Therefore aspect ratio AR; in particular as the torque density increases, the AR increases as well. The distribution of the losses is practically the same between iron and joule losses.

This design step has been carried out with an optimization that perform 3000 functional evaluations (50 individuals iterated over 60 generations); each individual takes 10 s to be evaluated, leading to a total computational time of 8.5 hours.

Solution number 3 has been selected as the initial design of the second refinement design stage described in the next section.

Table II: Design variables of the selected solutions

Design	D_{sc} [mm]	L_{stk} [mm]	SR [p.u.]	k_{air} [p.u.]	l_i [p.u.]	w_i [p.u.]
1	320	70	0.556	0.42	0.54	0.56
2	300	70	0.556	0.44	0.54	0.56
3	290	70	0.556	0.45	0.54	0.58
4	280	70	0.556	0.45	0.52	0.6

B. Average torque, torque ripple optimization

During the first design stage, the main stator parameters have been identified with the aim of obtaining the highest torque density with the minimum losses without considering the torque ripple. In the second design step the latter is improved acting on the geometrical variables which mainly influence the torque profile,

The latter, compared with the initial machine shows a reduction of the torque ripple from 44% to 8%, is worth to highlight how the refinement optimization have taken to an improvement of the torque ripple without affecting the average torque. Table IV summarizes the design variables of the final machine as well as the variables of the initial machine.

It is clear that the angular position at the airgap of the flux barriers and the slot opening width play a key role in the torque ripple minimization. In fact, they significantly influence the torque ripple and almost do not affect the average torque. This design step has been carried out with an optimization that perform 2400 functional evaluations (40 individuals iterated over 60 generations); each individual takes 10 s to be evaluated, leading to a total computational time of 6.5 hours. Fig. 5 depict the flux density distribution of the optimal machine with the maximum values highlighted.

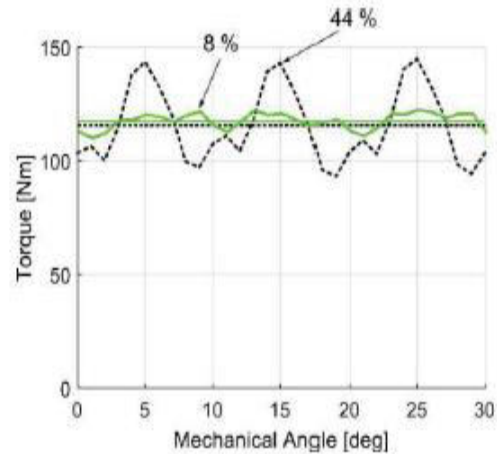


Figure : Pareto front of the second design step: average torque - torque ripple optimization.

Table IV : Design variables of the initial and final solutions

Design	k_{air} [p.u.]	α_1 [deg.]	α_2 [deg.]	α_3 [deg.]	so [p.u.]
Initial	0.45	18.8	28	38	0.3
Final	0.42	15.3	27.1	39.2	0.64

4 Constant power speed range improvements It is well known that the insertion of permanent magnets inside the rotor flux barriers improves the constant power speed range as well as the power factor. [deally an infinite CPSR is achieved if the following equations is satisfied [refl :

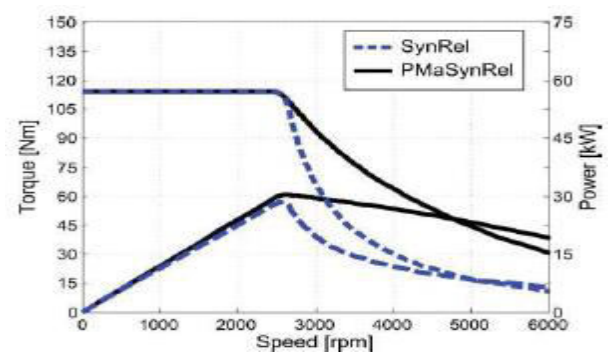


Figure 7: Electromechanical performance: Torque and Power vs speed characteristics.

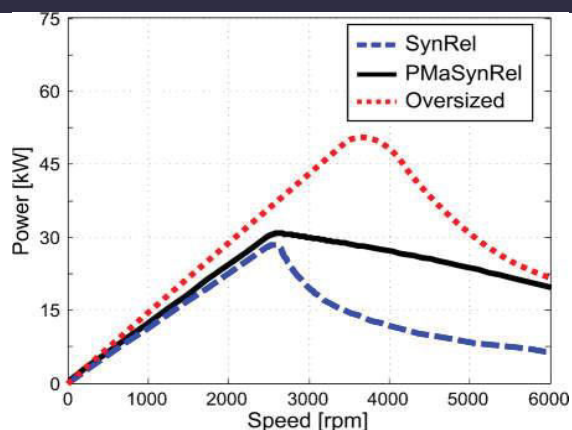


Figure 8: Power vs speed characteristics comparison with SynRel oversized.

Conclusions

This paper presents an automated design procedure of asynchronous reluctance machine having the aim of optimizing the torque density, the losses and the torque ripple. The methodology makes use of a stochastic optimization algorithm and finite element analysis. Particular attention has been paid to reduce the computational burden through a careful subdivision of the design procedure. This consists in two steps: first the main parameters affecting torque density and losses are optimized by a means of static FE simulations while in the second step, the variables which mainly influence the torque ripple are optimized through transient FE simulation. It has been proved that such approach considerably decreases the computational time and the goal of reducing the torque ripple has been achieved. Moreover, the comparison between the PMaSynRel and a pure SynRel machine having the same power at maximum speed shows that the latter needs a 40% increment in terms of overall volume.

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